

## Reading/Blogging Assignments

Come to class on

1. Friday having tried to square a rectangle and square a triangle.
2. Monday having read and blogged on section 3.2 up to **Discussion** on p. 43.
3. Wednesday having read and blogged on the rest of section 3.2
4. Friday having read and blogged on 3.3.

## Problem Set 6, Due October 15

Feel free to do some experimentation via a computer algebra system to develop intuition for the problem.

1. Problem 5 in the notes. Also show that, for example,  $\mathbb{Q}(\sqrt{3}, \sqrt{5}) = \mathbb{Q}(\sqrt{3} + \sqrt{5})$ . Can you generalize this result? (10 points)
2. Prove that the square roots of all prime numbers are linearly independent over  $\mathbb{Q}$ . Deduce that algebraic extensions need not be finite. (10 points)
3. Let  $L/K$  be a finite extension and let  $f$  be an irreducible polynomial over  $K$ . Show that if  $\deg f$  and  $[L : K]$  are coprime, then  $f$  has no zeros in  $L$  (3 points)
4. Problems 9 and 10 in the notes (10 points).